# Structural Analysis of the Orthorhombic Room- and Low-Temperature Phases of $\left[\mathrm{N}\left(\mathrm{CH}_{3}\right)_{4} \mathrm{I}_{2} \mathrm{ZnI}_{4}\right.$ 

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#### Abstract

Bis(tetramethylammonium) tetraiodozincate (TMA$\mathrm{ZnI}_{4}$ ) exhibits two successive structural transitions of first and second order at 218 and 255 K , respectively. The crystal structures of phase I (room temperature) and of phase III ( 150 K ) have been determined by X-ray diffraction. The high-temperature phase I has a $\beta-\mathrm{K}_{2} \mathrm{SO}_{4}$-type structure with an orientational disorder of the TMA groups. In phase III, the crystal structure is commensurately modulated by an ordered displacement of the rigid $\mathrm{ZnI}_{4}$ tetrahedra and TMA groups. The modulation direction is perpendicular to the pseudohexagonal axis, an orientation which is specific to this compound. Crystal data of phase $\mathrm{I}: M_{r}=691 \cdot 0$, Pmcn, $a=9.639(9), b=$ 16.722 (4) , $c=13.254$ (6) $\AA, V=2163$ (3) $\AA^{3}, Z=4$, $D_{x}=2.24 \mathrm{~g} \mathrm{~cm}^{-3}, \quad \lambda($ Mo $K \alpha)=0.7107 \AA, \quad \mu=$ $70.2 \mathrm{~cm}^{-1}, \quad F(000)=1312, \quad R=0.045$ for 1276 observed reflections. Crystal data of phase III: $M_{r}=$ $721.28, \quad P b c 2_{1}, \quad a=9.574$ (3),$\quad b=33.020$ (6),$\quad c=$ $13 \cdot 106(3) \AA, \quad V=4143(3) \AA^{3}, \quad Z=8, \quad D_{x}=$ $2.31 \mathrm{~g} \mathrm{~cm}^{-3}, \lambda($ Мо $K \alpha)=0.7107 \AA, \mu=71.01 \mathrm{~cm}^{-1}$, $F(000)=2624, \quad R=0.041$ for 2886 observed reflections.


## 1. Introduction

A considerable number of compounds of the type $\left[\mathrm{N}\left(\mathrm{CH}_{3}\right)_{4}\right]_{2} B X_{4}$ have been the subject of recent studies (Axe, 1986). They belong to the $A_{2} B X_{4}$ family whose members undergo a series of ferroic and displacive phase transitions and show similar behaviour. All compounds under consideration adopt the same normal (high-temperature) structure of the $\beta-\mathrm{K}_{2} \mathrm{SO}_{4}$ type. This structure is pseudohexagonal with the space group Pmcn. It is customary to choose $\mathbf{c}$ to describe the pseudohexagonal axis.

A variety of successive phase transitions which may lead to commensurate or incommensurate structures take place in these compounds. In general, the
wavevector of the modulation is along the $c^{*}$ direction. Most of them have been united in a common pressure-temperature diagram (Gesi, 1986) describing their sequence of phase transitions.

In contrast, the newly discovered compounds $\left[\mathrm{N}\left(\mathrm{CH}_{3}\right)_{4}\right]_{2} \mathrm{CuBr}_{4}$ (Hasebe, Mashiyama \& Tanisaki, 1985; Gesi, 1982), $\left[\mathrm{N}\left(\mathrm{CH}_{3}\right)_{4}\right]_{2} \mathrm{CdI}_{4}$ (Kallel, Bats \& Daoud, 1981; Werk \& Chapuis, 1988) and $\left[\mathrm{N}\left(\mathrm{CH}_{3}\right)_{4}\right]_{2} \mathrm{ZnI}_{4}$ (henceforth TMA- $\mathrm{ZnI}_{4}$ ) (Werk, Chapuis \& Perret, 1987) exhibit a sequence of transitions which does not follow this general phase diagram, since they develop modulations perpendicular to the pseudohexagonal axis in the $\mathbf{b}^{*}$ direction. This common feature constitutes a new subgroup of phases of the TMA- $B X_{4}$ family.
In TMA- $\mathrm{CuBr}_{4}$ the modulation wavevector of the incommensurate phase is $\mathbf{q}=\left(\frac{1}{2}-\delta\right) \mathbf{b}^{*}$. On lowering the temperature, a lock-in transition results in a ferroelectric commensurate phase with $\delta=0$ and space group $\mathrm{Pbc} 2_{1}$. On further cooling, another commensurate structure with space group $P 12_{1} / c l$ is found (Hasebe, Mashiyama \& Tanisaki, 1982). Structural analyses of the normal and the lock-in phases have been reported (Trouelan, Lefebvre \& Derollez, 1984; Hasebe et al., 1985). The thermodynamics of the phase-transition sequences have been studied by Lopez-Echarri, Ruiz-Larrea \& Tello (1988).

At normal pressure, the title compound TMA$\mathrm{ZnI}_{4}$ exhibits two phase transitions below room temperature. Besides the normal phase (I), a ferroelastic phase (II) (Hasebe, Asahi \& Gesi, 1990) is found which transforms into a commensurate phase (III). Studies of the dielectric properties (Gesi \& Perret, 1988) indicate that phase III is of the so-called improper ferroelectric type. This term is used to indicate that the ferroelectric state does not disappear with decreasing temperature. This is in contrast to the other TMA- $B X_{4}$-type ferroelectrics in which the ferroelectric state exists only in a limited temperature range.

We report in this paper a study of TMA- $\mathrm{ZnI}_{4}$ with modulations along the $\mathbf{b}^{*}$ direction. In particular, we present analyses obtained from differential scanning calorimetry (DSC), optical microscopy and singlecrystal X-ray studies. The structures of the phases I and III are reported. As previously observed for other $\beta$ - $\mathrm{K}_{2} \mathrm{SO}_{4}$-type compounds, the normal phase was found to be disordered $\left(\mathrm{Rb}_{2} \mathrm{ZnCl}_{4}\right.$, Itoh, Hinasada, Daika, Ando \& Nakamura, 1986; $\mathrm{Rb}_{2} \mathrm{ZnBr}_{4}$, de Pater, Axe \& Currat, 1979; TMA$\mathrm{CuBr}_{4}$, Hasebe et al., 1985; and others). In TMA$\mathrm{ZnI}_{4}$ an order-disorder process was associated with the structural transition from phase I to III.

## 2. Experimental

Synthesis. Transparent crystals of TMA- $\mathrm{ZnI}_{4}$ were grown by evaporation at room temperture of an aqueous hypophosphorous acid solution containing $\left(\mathrm{CH}_{3}\right)_{4} \mathrm{~N}^{+} . \mathrm{I}^{-}$and $\mathrm{ZnI}_{2}$ in the molar ratio $1: 10$. Single-crystal X-ray studies confirmed the identity of the compound.

DSC and polarized-light microscopy. Calorimetric studies have shown that TMA- $\mathrm{ZnI}_{4}$ undergoes two phase transitions at 255 and 218 K (Arend, 1986; M. L. Werk, unpublished results). Both transitions were reversible. The peak-shape anomalies indicate that the transitions are of second and first order, respectively.

This finding is in agreement with results obtained using polarized-light microscopy (Werk, Chapuis \& Schmid, 1987). Observations on (100)-cut platelets of TMA- $\mathrm{ZnI}_{4}$ at room temperature showed the orthorhombic phase I optically monodomain. The secondorder phase transition from phase I to phase II is accompanied by the appearance of unstable, narrow ferroelastic domains. In phase II, the birefringence increased continously with decreasing temperature. The occurrence of domains strongly indicated a symmetry reduction, probably from orthorhombic to monoclinic. The transition from phase II to phase III is characterized by a sharp decrease in birefringence and a return to optical homogeneity. This transition behaviour was reversible with a hysteresis of about $5^{\circ}$.
$X$-ray diffraction. At room temperature, the intensity distribution of single-crystal photographs indicated the presence of the normal $\beta-\mathrm{K}_{2} \mathrm{SO}_{4}$-type structure. The space group is Pmen if we postulate a centre of symmetry as confirmed later by refinement. In phase III, below 220 K , commensurate superstructure reflections appeared which result in a doubling of the lattice parameter $b$. This phase is orthorhombic and the systematic absences indicate the diffraction symbol $P b c^{*}$. Packing considerations and the assumption that phase III is a minor distortion of phase I favoured the polar space group $\mathrm{Pbc} 2_{1}$.

Spontaneous polarization effects observed by pyroelectric charge measurements (Gesi \& Perret, 1988) confirmed the polar character of phase III.

Data collection. X-ray measurements were carried out on an Enraf-Nonius CAD-4 four-circle diffractometer. Intensities of phases I and III were each measured on a different specimen. Phase III was identified by the appearance of the superstructure reflections. During the measurement of phase III the crystal was cooled to $\cong 150 \mathrm{~K}$ by an open stream of nitrogen gas. The temperature was controlled by a thermocouple positioned a few millimeters from the crystal. Temperature fluctuations at the thermocouple were less than $1^{\circ}$. Experimental details of the measurements are given in Table 1.

### 2.1. Structure refinement

All calculations were performed with the $X R A Y 72$ system of programs (Stewart, Kruger, Ammon, Dickinson \& Hall, 1972) Atomic scattering factors for neutral atoms were taken from Cromer \& Mann (1968) and the dispersion corrections were those of Cromer \& Liberman (1970).

Normal phase (phase I). The structure of the normal phase was refined with the starting parameters for the Zn and I atoms of the isomorphous compound TMA- $\mathrm{ZnCl}_{4}$ (Wiesner, Srivastava, Kennard, Di Vaira \& Lingafelter, 1967). Difference Fourier maps revealed all C and N atoms. Refinements were carried out by full-matrix least squares, including anisotropic displacement parameters for all atoms. In the final cycles, an extinction parameter was also refined. In the refinement, the $\mathbf{C}$ atoms exhibited large anisotropic thermal parameters $U_{i j}$. This result indicates an orientational disorder of the $\mathrm{NC}_{4}$ tetrahedra rather than thermal displacements. Only $U_{i j}$ of the $\mathrm{C}(21)$ atom and the N atoms have smaller values. This suggests a rotational disorder of the $\mathrm{NC}_{4}$ tetrahedra which deviates from the average orientation. A model was introduced with disordered $\mathrm{NC}_{4}$ tetrahedra symmetrically distributed on two equivalent positions. The anisotropic refinement is also indicative of a displacement of the $\mathrm{ZnI}_{4}$ tetrahedra, but too small to justify atomic separation.

Phase III. During intensity measurements of phase III, significant variations of the intensity-control reflections were observed owing to technical problems. The data were scaled correspondingly. Refinement was started from the positional parameters for the Zn and I atoms obtained for the normal phase and transformed to the base vectors of the superstructure cell.

The remaining coordinates for the N and C atoms were obtained from a difference Fourier map. Refinement of the enantiomorph-polarity parameter (Flack, 1983) was used to determine the orientation

Table 1. Data on the structure determinations of $\left[\mathrm{N}\left(\mathrm{CH}_{3}\right)_{4}\right]_{2} \mathrm{ZnI}_{4}$

|  | Phase I | Phase III |
| :---: | :---: | :---: |
| Temperature ( K ) | 293 | 150 |
| Space group | Pmen | Pbc ${ }_{1}$ |
| $a(\AA)$ | 9.668 (9) | 9.574 (3) |
| $b(\AA)$ | 16.765 (4) | 33.020 (6) |
| $c(\AA)$ | 13.303 (6) | 13.106 (3) |
| $V\left(\AA^{3}\right)$ | 2156 (3) | 4143 (3) |
| $Z$ | 4 | 8 |
| $D_{x}\left(\mathrm{~g} \mathrm{~cm}^{-3}\right)$ | 2.24 | 2.31 |
| $F(000)$ | 1312 | 2624 |
| $\lambda($ Mo $K \alpha)(\AA)$ | 0.7107 | 0.7107 |
| Monochromator | Graphite | Graphite |
| No. of reflections used for lattice parameters | 15 | 20 |
| $\theta$ range for lattice parameters (") | 10-20 | 10-24 |
| Scan width | $(0.65+0.34 \tan \theta)^{\circ}$ | $(0.8+0.34 \tan \theta)^{\circ}$ |
| Scan speed ( $\mathrm{min}^{-1}$ ) | Variable, 2-10 | Variable, 1.65-10 |
| Scan mode | $\omega / 2 \theta$ | $\omega$ |
| Range of $h k l$ | $0 \leq h \leq 13$ | $-10 \leq h \leq 10$ |
|  | $\begin{aligned} & 0 \leq k \leq 23 \\ & -18 \leq 1 \leq 18 \end{aligned}$ | $\begin{aligned} & -35 \leq k \leq 35 \\ & 0 \leq l \leq 14 \end{aligned}$ |
| Orientation control reflections (period) | 3 (every 70 reflections) | 3 (every 100 reflections) |
| Intensity control reflections (period) | 3 (every 70 reflections) |  |
| $(\sin \theta / \lambda)_{\text {max }}\left(\AA^{-1}\right)$ | 0.7050 | $0.5493$ |
| Collected reflections | 5837 | 6051 |
| Non-equivalent reflections | 3273 | 3028 |
| Reflections with $I>3 \sigma(I)$ | 1276 | 2886 |
| $\mu$ (Mo K $\alpha$ ) (cm ${ }^{1}$ ) | $70 \cdot 2$ | 71.01 |
| Crystal faces | $\begin{aligned} & (010),(0 T 0),(20 \mathrm{~T}) \\ & (\mathrm{T} 00),(\mathrm{T} \mid \mathrm{T}),(1 \mathrm{~T} 13) \end{aligned}$ | \{100\}, 2010$\},\{001\}$ |
| Approximate crystal dimensions (mm) | $0.21 \times 0.25 \times 0.24$ | $0.44 \times 0.15 \times 0.15$ |
| Min./max. transmission | $0.188 / 0.303$ | 0.349/0.408 |
| $R_{\text {int }}$ | - | 0.028 |
| Reflections used | All | All |
| Extinction correction | Yes | No |
| $R$ | 0.045 | 0.041 |
| $w R$ | 0.060 | 0.045 |
| Weight function | $1 / \sigma^{2}(F)$ | $1 / \sigma^{2}(F)$ |
| Max. shift/e.s.d. in final least-squares cycle | - | 0.075 |
| No. of parameters |  |  |
| Variables | 136 | 465 |
| Soft restrictions | 0 | 208 |

of the polar axis. Anisotropic displacement parameters were assigned to all atoms. The origin of the coordinate system along $\mathbf{c}$ was fixed using the method of Flack \& Schwarzenbach (1988).

In the final refinement cycles, H -atom positions were calculated assuming $\mathrm{N}-\mathrm{CH}_{3}$ tetrahedra with ideal cubic symmetry and a $\mathrm{C}-\mathrm{H}$ bond length of $1 \AA$. The resulting H -atom coordinates were refined using distances and rigid-bond restraints (Schwarzenbach \& Didisheim, 1987). H-atom displacements were assumed to be isotropic. The weight of each restraint corresponded to the reciprocal value of the standard deviation for the prescribed rigid bond. Assumed e.s.d.'s for rigid-bond restraints were $\mathrm{N}-\mathrm{C}=0.0$ and $\mathrm{C}-\mathrm{H}=0.0$; distances were restrained such that $\mathbf{C}-\mathrm{H}=1$. In the last step it was multiplied by ten in order to release the constraints. Because of limitations of the available computer memory, the least-squares matrix was subdivided into four blocks. One block included the atom parameters of the $\mathrm{ZnI}_{4}$ tetrahedra and each of the remaining blocks contained one TMA group.

Table 2. Fractional atomic coordinates $\left(\times 10^{4}\right)$, population factors (pp) and equivalent isotropic displacement parameters $\left(\AA^{2} \times 10^{4}\right)$

|  | $x$ | $y$ | $z$ | $p p$ | $U_{\text {eq }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| (a) Normal phase 1 l ${ }^{\text {a }}$ |  |  |  |  |  |
| Zn | 2500 | $4073 \cdot 8$ (7) | 2541.3 (8) |  | 674 (7) |
| 1(1) | 2500 | 3989 (5) | 580.8 (5) |  | 970 (6) |
| 1(2) | 2500 | 5538.7 (5) | 3183 (7) |  | 1173 (7) |
| 1(3) | $284 \cdot 1$ (8) | 3363.3 (5) | 3225.6 (5) |  | 1214 (6) |
| N(1) | 2500 | 1005 (6) | 1516 (6) |  | 76 (3) |
| C(11) | 1910 (30) | 910 (20) | 2520 (10) | 0.5 | 1600 (100) |
| C(12) | 3320 (50) | 1660 (20) | 1320 (40) | 0.5 | 1900 (200) |
| C(13) | 3020 (20) | 210 (10) | 1080 (20) | 0.5 | 1500 (100) |
| C(14) | 1220 (40) | 1250 (30) | 1000 (30) | 0.5 | 2400 (300) |
| N(2) | 2500 | 8341 (5) | 4749 (6) |  | 710 (30) |
| C(21) | 2500 | 7543 (9) | 4380 (10) |  | 1570 (900) |
| C(22) | 1040 (30) | 8530 (10) | 5030 (30) | 0.5 | 1700 (200) |
| C(23) | 3220 (30) | 8340 (20) | 5680 (20) | 0.5 | 1600 (200) |
| C(24) | 3010 (20) | 8920 (10) | 4000 (10) | 0.5 | 1100 (100) |
| (b) Phase III |  |  |  |  |  |
| $\mathrm{Zn}(1)$ | 2044 (2) | 2031.9 (6) | 2176 (2) |  | 280 (9) |
| 1(11) | 2448 (1) | $1973 \cdot 8$ (4) | 199.6 (9) |  | 342 (7) |
| I(12) | 1633 (1) | 2773.8 (3) | 2773 (1) |  | 404 (7) |
| I(13) | -166 (1) | 1593.4 (3) | 2642 (1) |  | 382 (7) |
| I(14) | 4264 (1) | 1749.0 (4) | 3104 (1) |  | 412 (7) |
| $\mathrm{Zn}(2)$ | 7385 (2) | 2984.0 (6) | 7069 (2) |  | 293 (9) |
| 1(21) | 7246 (1) | 2994.0 (4) | 9071.9 (8) |  | 332 (7) |
| 1(22) | 7204 (1) | $2245 \cdot 3$ (3) | 6389 (1) |  | 465 (7) |
| I(23) | 5320 (1) | 3408.5 (4) | 6321 (1) |  | 442 (7) |
| 1(24) | 9780 (1) | $3301 \cdot 1$ (4) | 6499 (1) |  | 405 (7) |
| N(1) | 7950 (10) | 4500 (4) | 8090 (10) |  | 330 (40) |
| C(11) | 7530 (20) | 4900 (6) | 8520 (20) |  | 900 (100) |
| H(111) | 8100 (100) | 4960 (20) | 9140 (60) |  | 900 (300) |
| H(112) | 7700 (100) | 5115 (8) | 7990 (50) |  | 1700 (300) |
| H(113) | 6520 (40) | 4890 (20) | 8700 (100) |  | 600 (200) |
| C(12) | 9470 (20) | 4450 (6) | 8240 (20) |  | 800 (100) |
| H(121) | 9980 (30) | 4610 (30) | 7700 (70) |  | 900 (200) |
| $\mathrm{H}(122)$ | 9740 (40) | 4560 (40) | 8930 (50) |  | 900 (200) |
| H(123) | 9720 (40) | 4157 (9) | 8200 (100) |  | 900 (200) |
| C(13) | 7220 (20) | 4177 (7) | 8600 (20) |  | 900 (100) |
| H(131) | 6200 (30) | 4190 (30) | 8430 (80) |  | 600 (200) |
| H(132) | 7600 (100) | 3910 (6) | 8370 (80) |  | 1800 (300) |
| H(133) | 7300 (100) | 4200 (30) | 9360 (20) |  | 800 (200) |
| C(14) | 7570 (20) | 4484 (7) | 6960 (10) |  | 640 (90) |
| H(141) | 7700 (100) | 4200 (10) | 6700 (30) |  | 900 (200) |
| H(142) | 6570 (40) | 4560 (30) | 6870 (20) |  | 600 (200) |
| H(143) | 8170 (90) | 4680 (30) | 6580 (20) |  | 800 (200) |
| N(2) | 2170 (20) | 487 (4) | 1140 (10) |  | 390 (50) |
| C(21) | 3250 (20) | 813 (6) | 1250 (20) |  | 730 (90) |
| H(211) | 3960 (80) | 730 (20) | 1770 (80) |  | 900 (200) |
| H(212) | 3700 (100) | 860 (30) | 580 (30) |  | 700 (200) |
| H(213) | 2790 (40) | 1070 (10) | 1500 (100) |  | 800 (200) |
| C(22) | 2870 (20) | 103 (6) | 780 (20) |  | 620 (90) |
| H(221) | 3200 (100) | 140 (10) | 50 (30) |  | 500 (200) |
| H(222) | 3700 (80) | 50 (20) | 1210 (60) |  | 900 (200) |
| H(223) | 2200 (60) | - 128 (9) | 830 (80) |  | 600 (200) |
| C(23) | 1080 (30) | 623 (9) | 390 (20) |  | 1100 (100) |
| H(231) | 600 (100) | 380 (10) | 100 (100) |  | 1700 (300) |
| H(232) | 400 (100) | 810 (40) | 730 (40) |  | 1400 (300) |
| H(233) | 1540 (40) | 770 (40) | -190 (60) |  | 900 (200) |
| C(24) | 1510 (20) | 423 (6) | 2140 (10) |  | 670 (90) |
| H(241) | 1200 (100) | 690 (10) | 2420 (50) |  | 700 (200) |
| H(242) | 700 (80) | 240 (30) | 2060 (30) |  | 900 (200) |
| H(243) | 2210 (50) | 300 (40) | 2620 (30) |  | 800 (200) |
| N(3) | 2490 (10) | 4210 (4) | 4380 (10) |  | 310 (40) |
| C(31) | 1670 (20) | 4252 (6) | 5330 (10) |  | 540 (80) |
| H(311) | 1950 (80) | 4040 (20) | 5820 (30) |  | 600 (200) |
| H(312) | 650 (20) | 4220 (30) | 5170 (20) |  | 600 (200) |
| H(313) | 1840 (90) | 4520 (10) | 5640 (50) |  | 600 (200) |
| C(32) | 2380 (20) | 3790 (6) | 4000 (10) |  | 560 (80) |
| H(321) | 1410 (50) | 3740 (10) | 3740 (90) |  | 700 (200) |
| H(322) | 2600 (100) | 3599 (6) | 4580 (30) |  | 600 (200) |
| H(323) | 3070 (90) | 3750 (10) | 3440 (70) |  | 700 (200) |
| C(33) | 1880 (20) | 4499 (5) | 3600 (10) |  | 420 (70) |
| H(331) | 2420 (70) | 4480 (20) | 2950 (30) |  | 400 (100) |
| H(332) | 1950 (90) | 4782 (6) | 3870 (40) |  | 600 (100) |
| H(333) | 880 (30) | 4430 (20) | 3480 (50) |  | 300 (100) |
| C(34) | 3960 (20) | 4318 (6) | 4540 (10) |  | 450 (60) |
| H(341) | 4030 (30) | 4610 (10) | 4770 (70) |  | 600 (100) |
| H(342) | 4500 (30) | 4280 (30) | 3890 (30) |  | 400 (100) |
| H(343) | 4370 (40) | 4140 (20) | 5080 (60) |  | 400 (100) |
| N(4) | 7200 (10) | 821 (4) | 4840 (10) |  | 320 (40) |
| C(41) | 7220 (20) | 1260 (6) | 5150 (10) |  | 490 (60) |

Table 2 (cont.)

|  | $x$ | $y$ | $z$ | $p p$ | $U_{\text {eq }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| H(411) | 7790 (90) | 1290 (10) | 5780 (50) |  | 400 (100) |
| H(412) | 6240 (30) | 1350 (10) | 5280 (80) |  | 500 (100) |
| H(413) | 7600 (100) | 1425 (7) | 4590 (40) |  | 700 (200) |
| C(42) | 6630 (20) | 570 (5) | 5670 (10) |  | 390 (60) |
| H(421) | 5680 (50) | 670 (20) | 5860 (50) |  | 400 (100) |
| H(422) | 7260 (60) | 580 (20) | 6280 (30) |  | 400 (100) |
| H(423) | 6550 (90) | 282 (8) | 5440 (30) |  | 500 (100) |
| C(43) | 6330 (20) | 778 (5) | 3890 (10) |  | 490 (70) |
| H(431) | 6350 (90) | 490 (9) | 3650 (50) |  | 400 (100) |
| H(432) | 6720 (70) | 960 (20) | 3340 (30) |  | 600 (100) |
| H(433) | 5350 (30) | 860 (30) | 4040 (30) |  | 700 (200) |
| C(44) | 8660 (20) | 690 (5) | 4640 (10) |  | 440 (60) |
| H(441) | 9060 (40) | 860 (20) | 4080 (60) |  | 500 (100) |
| H(442) | 8670 (30) | 400 (10) | 4440 (80) |  | 500 (100) |
| H(443) | 9230 (30) | 730 (30) | 5270 (30) |  | 600 (200) |

Symmetry transformations: $x, y, z ;-x+\frac{1}{2},-y-\frac{1}{4}, \frac{1}{2}+z ;-x+\frac{1}{2}, y+\frac{1}{2}, z ;$ $x, \frac{1}{4}-y, z+\frac{1}{2}$.

Final values of the reliability factors were $R=$ $0.041, w R=0.045$. The maximum shift/e.s.d. after the final least-squares cycle was 0.075 . In the final difference Fourier map the residual maxima were $2 \cdot 1 \mathrm{e} \AA^{-3}$, at a distance of $0.89 \AA$ from I.

Final atomic positional and equivalent isotropic displacement parameters of phases I and III are listed in Tables $2(a)$ and $2(b)$. Tables $3(a)$ and $3(b)$ list important distances for the two phases.*

## 3. Results and discussion

Crystal structure of the normal phase. The structure of the normal phase shows that TMA- $\mathrm{ZnI}_{4}$ indeed belongs to the $A_{2} B X_{4}$ family. Structural units are isolated $\mathrm{NC}_{4}$ tetrahedra and $\mathrm{ZnI}_{4}$ tetrahedra. Several descriptions of normal $\mathrm{K}_{2} \mathrm{SO}_{4}$-type structures can be found in the literature (Axe, 1986, and references cited therein). The disordered arrangement of the tetrahedra seems to be an important characteristic feature of these compounds (Wiesner et al., 1967; Matsunaga, 1982; Hasebe et al., 1985; Perret, Godefroy \& Arend, 1987).

Figs. 1 and 2 show the contents of the unit cell of TMA- $\mathrm{ZnI}_{4}$ projected onto ( 001 ). In the ideal structure, all tetrahedra are located on planes normal to a. At $x=\frac{1}{4}$, the $\mathrm{ZnI}_{4}$ tetrahedra point downwards along - $\mathbf{c}$ and at $x=\frac{3}{4}$ they point upwards along $+\mathbf{c}$. The $\mathrm{NC}_{4}$ tetrahedra at $x=\frac{1}{4}$ and $x=\frac{3}{4}$ are arranged alternately. The tetrahedra are located on mirror planes. Furthermore, all tetrahedra can be considered to lie on four different layers normal to $\mathbf{c}$. Two layers at $z=\frac{1}{4}$ and $z=\frac{3}{4}$ are occupied by $\mathrm{ZnI}_{4}$ and $\mathrm{NC}_{4}$ tetrahedra. The remaining layers at $z=0$ and $z=\frac{1}{2}$ contain only $\mathrm{NC}_{4}$ tetrahedra.

[^0]Table 3. Selected interatomic distances $(\AA)$ and bond angles $\left({ }^{\circ}\right)$ with e.s.d.'s in parentheses

| Bond lengths for phase I are given without and with (second column) corrections for thermal motion. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| (a) Normal phase I |  |  |  |  |
| $\mathrm{Zn}-1(1)$ | $2 \cdot 602$ (2) | $2 \cdot 623$ | 1(1)-2n-1(2) | $112 \cdot 28$ (5) |
| 1(2) | 2.593 (2) | $2 \cdot 622$ | $1(1)$ I(3) | 108.82 (4) |
| 1(3) | 2.607 (2) | 2.639 | $1(2) \quad 1(3)$ | 108.44 (4) |
| $\mathrm{N}(1)-\mathrm{C}(11)$ | 1.45 (2) | 1.55 | $\mathrm{C}(11)-\mathrm{N}(1)-\mathrm{C}(12)$ | 119 (2) |
| $\mathrm{C}(12)$ | $1 \cdot 38$ (4) | 1.48 | $\mathrm{C}(11) \quad \mathrm{C}(13)$ | 112 (1) |
| C(13) | 1.53 (2) | 1.63 | $\mathrm{C}(11) \quad \mathrm{C}(14)$ | 97 (2) |
| C(14) | 1.46 (4) | 1.59 | $\mathrm{C}(12) \quad \mathrm{C}(13)$ | 115 (2) |
|  |  |  | $\mathrm{C}(12) \quad \mathrm{C}(14)$ | 100 (3) |
|  |  |  | $\mathrm{C}(13) \quad \mathrm{C}(14)$ | 110 (2) |
| $\mathrm{N}(2)-\mathrm{C}(21)$ | 1.42 (2) | 1.49 | $\mathrm{C}(21)-\mathrm{N}(2)-\mathrm{C}(22)$ | 107 (1) |
| C(22) | 1.49 (3) | 1.58 | $\mathrm{C}(21) \quad \mathrm{C}(23)$ | 107 (1) |
| C(23) | 1.42 (3) | 1.51 | $\mathrm{C}(21) \quad \mathrm{C}(24)$ | 113 (1) |
| C (24) | 1.48 (2) | 1.51 | $\mathrm{C}(22) \quad \mathrm{C}(23)$ | 104 (2) |
|  |  |  | $\mathrm{C}(22) \quad \mathrm{C}(24)$ | 110 (1) |
|  |  |  | C(23) C(24) | 115 (1) |
| (b) Phase III |  |  |  |  |
| $\mathrm{Zn}(1)-\mathrm{l}(11)$ | 2.626 (3) |  | $\mathrm{I}(11)-\mathrm{Zn}(1)-\mathrm{I}(12)$ | 112.80 (9) |
| I(12) | 2.601 (2) |  | $1(11) \quad 1(13)$ | 107.86 (9) |
| 1(13) | 2.635 (2) |  | 1(1) I(14) | 108.17 (8) |
| I(14) | $2 \cdot 621$ (3) |  | $1(11) \quad \mathrm{I}$ (13) | 109.05 (8) |
|  |  |  | $\mathrm{l}(12) \quad 1(14)$ | 108.61 (9) |
|  |  |  | $1(13) \quad 1(14)$ | $110 \cdot 35$ (9) |
| $\mathrm{Zn}(2)-1(21)$ | 2.628 (3) |  | 1(21)-Zn(2)-1(22) | 110.51 (8) |
| $1(22)$ | $2 \cdot 602$ (2) |  | $1(21) \quad 1(23)$ | 109.25 (9) |
| 1(23) | 2.615 (3) |  | $1(21) \quad \mathrm{I}(24)$ | 108.85 (9) |
| $1(24)$ | 2.629 (3) |  | $1(22) \quad 1(23)$ | 108.88 (9) |
|  |  |  | $1(22) \quad I(24)$ | 109.51 (9) |
|  |  |  | $1(23) \quad \mathrm{l}(24)$ | 109.83 (8) |
| $\mathrm{N}(1)-\mathrm{C}(11)$ | 1.46 (2) |  | $\mathrm{C}(11)-\mathrm{N}(1)-\mathrm{C}(12)$ | 108 (1) |
| $\mathrm{C}(12)$ | 1.49 (2) |  | $\mathrm{C}(11) \quad \mathrm{C}(13)$ | 111 (1) |
| C(13) | 1.51 (2) |  | $\mathrm{C}(11) \quad \mathrm{C}(14)$ | 109 (1) |
| C(14) | 1.51 (3) |  | $\mathrm{C}(12) \quad \mathrm{C}(13)$ | 109 (1) |
|  |  |  | $\mathrm{C}(12) \quad \mathrm{C}(14)$ | 109 (1) |
|  |  |  | $\mathrm{C}(13) \quad \mathrm{C}(14)$ | 110 (1) |
| $\mathrm{N}(2)-\mathrm{C}(21)$ | 1.47 (2) |  | $\mathrm{C}(21)-\mathrm{N}(2)-\mathrm{C}(22)$ | 110 (1) |
| C(22) | 1.48 (2) |  | $\mathrm{C}(21) \quad \mathrm{C}(23)$ | 109 (1) |
| C(23) | 1.48 (2) |  | $\mathrm{C}(21) \quad \mathrm{C}(24)$ | 110 (1) |
| C(24) | 1.51 (2) |  | $\mathrm{C}(22) \quad \mathrm{C} 23)$ | 111 (1) |
|  |  |  | $\mathrm{C}(22) \quad \mathrm{C}(24)$ | 108 (1) |
|  |  |  | $\mathrm{C}(23) \quad \mathrm{C}(24)$ | 108 (1) |
| $\mathrm{N}(3)-\mathrm{C}(31)$ | 1.50 (2) |  | $\mathrm{C}(31)-\mathrm{N}(3)-\mathrm{C}(32)$ | 110 (1) |
| $\mathrm{C}(32)$ | 1.47 (2) |  | $\mathrm{C}(31) \quad \mathrm{C}(33)$ | 108 (1) |
| C(33) | 1.51 (2) |  | $\mathrm{C}(31) \quad \mathrm{C}(34)$ | 109 (1) |
| $\mathrm{C}(34)$ | 1.48 (2) |  | $\mathrm{C}(32) \quad \mathrm{C} 33)$ | 110 (1) |
|  |  |  | $\mathrm{C}(32) \quad \mathrm{C}(34)$ | 108 (1) |
|  |  |  | $\mathrm{C}(33) \quad \mathrm{C}(34)$ | 110 (1) |
| $\mathrm{N}(4)-\mathrm{C}(41)$ | $1 \cdot 49$ (2) |  | $\mathrm{C}(41)-\mathrm{N}(4)-\mathrm{C}(42)$ | 108 (1) |
| C(42) | 1.48 (2) |  | $\mathrm{C}(41) \quad \mathrm{C}(43)$ | 111 (1) |
| C(43) | 1.45 (3) |  | $\mathrm{C}(41) \quad \mathrm{C}(44)$ | 109 (I) |
| $\mathrm{C}(44)$ | 1.52 (2) |  | $\mathrm{C}(42) \cdot \mathrm{C}(43)$ | 110 (1) |
|  |  |  | $\mathrm{C}_{(42)}^{\mathrm{C}(44)}$ | 111 (1) |
|  |  |  | $\mathrm{C}(43) \quad \mathrm{C}(44)$ | 108 (1) |

In the final model adopted for the structure refinement, each $\mathrm{NC}_{4}$ tetrahedron is displaced from the mirror plane of the space group Pmen. The tetrahedra are essentially rotated about directions parallel to the $\mathbf{b}$ and $\mathbf{c}$ axes which cross their centres of gravity. It is not known whether the disorder is static or dynamic.

For all atoms of phase I (Table 2), the values are given with and without correction for thermal motion (Schomaker \& Trueblood, 1968). In phase I, the $\mathrm{Zn}-\mathrm{I}$ distances are shorter than in phase III, but become equal after correction for thermal motion.


Fig. 1. Phase $\mathrm{I}, \mathrm{ZnI}_{4}$ tetrahedra.


Fig. 2. (a) Phase I, $\mathrm{NC}_{4}$ tetrahedra, calculated average structure. (b) Phase I, NC 4 tetrahedra, refined positions.


Fig. 3. Phase III, $\mathrm{ZnI}_{4}$ tetrahedra. Rotations and translations of the rigid tetrahedra are indicated by arrows.


Fig. 4. Phase III, $\mathrm{NC}_{4}$ tetrahedra with displacements of the rigid tetrahedra.

Table 4. Displacements of the tetrahedra from the ideal structure with symmetry Pmcn for phase III

|  | $\mathrm{Zn}(1)$ | $\mathrm{Zn}(2)$ | $\mathrm{N}(1)$ | $\mathrm{N}(2)$ | $\mathrm{N}(3)$ | $\mathrm{N}(4)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $T_{x}$ | -0.046 | -0.012 | -0.033 | -0.001 | -0.030 | -0.045 |
| $R_{y}$ | 7 | 3 | 25 | 28 | 22 | 15 |
| $R_{z}$ | 6 | 6 | 13 | 3 | 5 | 18 |

Notes: $T_{x}=$ translation (relative units) of the cations along the $a$ axis. $R_{i}=$ rotation ( ${ }^{\circ}$ ) about an axis parallel to $i$.

### 3.1. Analysis of the displacements in the lowtemperature phase III

In phase III, the $\mathrm{ZnI}_{4}$ and $\mathrm{NC}_{4}$ tetrahedra are alternately displaced. Along the $\mathbf{b}$ direction two tetrahedra, which are equivalent in the normal phase, show an antiphase displacement in the superstructure. This leads to the doubling of the $b$ lattice constant and a transformation of the mirror plane of phase I into a glide plane (Figs. 3 and 4). A macroscopic dipole moment is created and the compound becomes ferroelectric (Gesi \& Perret, 1988). Table 3 shows that all the tetrahedra are quite regular. The deviations of their bond lengths and angles are much smaller than the displacements of the tetrahedra out of the mirror planes (Table 4). This confirms that the commensurate modulation of phase III consists mainly of displacements of rigid tetrahedral units. Their orientations characterize the different phases.

In order to discuss the structural change, the orientations of the tetrahedra in phase III will be compared with the ideal structure. Starting from the average structure, the modulated phase III results from the combination of three motions given in Table 4. Because the tetrahedra are nearly rigid, their translational displacements are represented by the displacements of the cations. The largest displacements are rotations of the tetrahedra about the $b$ and $\mathbf{c}$ directions. In addition, there is a small translation of the tetrahedra along the a direction.

The reason for the occurrence of the structural instability leading from phase I to phase III is not yet clear. Based on a semi-microscopic model, Janssen (1986) gives an explanation for the various commensurate and incommensurate modulated structures of the $\beta-\mathrm{K}_{2} \mathrm{SO}_{4}$ type and in particular of TMA- $B X_{4}$ compounds. The model is based on the competition of interactions between tetrahedra giving rise to a so-called 'structural frustration'. Janssen's (1986) approach was first formulated for structures with a modulation wavevector along the c direction. We believe, however, that the same mechanism may also be applied to the title compound.

Starting from the common basic structure, the model postulates displacive modulations of rigid tetrahedral units. In the basic structure, each $\mathrm{NC}_{4}$ tetrahedron has a pair of equivalent $\mathrm{ZnI}_{4}$ tetrahedra as first neighbours with the distance $a / 2$ parallel to a in the $a b$ plane. Intertetrahedral interactions favour
the approach of one corner of the $\mathrm{NC}_{4}$ tetrahedron to the Zn ion of one of the two nearest $\mathrm{ZnI}_{4}$ tetrahedra. These forces are antagonistic to the intertetrahedral repulsion forces, causing the tetrahedra to move to an equilibrium orientation. Fig. 5 shows an $a b$ layer at $z=0.25 . \mathrm{NC}_{4}$ and $\mathrm{ZnI}_{4}$ tetrahedra are displaced by rotations of equal sign about an axis parallel to $\mathbf{c}$, such that all corners of the $\mathrm{NC}_{4}$ tetrahedron point towards a face of the neighbouring $\mathrm{ZnI}_{4}$ tetrahedron. This configuration forms pseudohexagonal rings of $\mathrm{NC}_{4}$ and $\mathrm{ZnI}_{4}$ tetrahedra. All tetrahedra forming a ring are rotated in the same direction about $\mathbf{c}$ and commonly shifted parallel to $\mathbf{a}$. Neighbouring rings along $\mathbf{b}$ are rotated and shifted in the opposite directions. This is in contrast to compounds exhibiting modulations along $\mathbf{c}$, where the tetrahedra of an $a b$ layer are all displaced in a unique way. In phase III, the $\mathrm{NC}_{4}$ tetrahedra perpendicular to $\mathbf{c}$ at $z=0.0$ and $z=0.5$ are also displaced to an equilibrium position where corners of $\mathrm{ZnI}_{4}$ tetrahedra point towards faces of neighbouring $\mathrm{NC}_{4}$ tetrahedra.

In this structure, the displacements are essentially rotations of rigid tetrahedra. This behaviour is common to most of the other $A_{2} B X_{4}$ compounds (Hogervorst, 1986; Colla, 1988). Since the rotation of the tetrahedra is an obvious aspect of the structural phase transition, it has been chosen as the structural order parameter by Janssen (1986). We believe that the displacements of TMA-ZnI ${ }_{4}$ may also support this order parameter. But the specific orientation of the tetrahedra makes TMA- $\mathrm{ZnI}_{4}$ a remarkable case. In compounds exhibiting modulations along $\mathbf{c}$, the tetrahedra pointing upwards along $+\mathbf{c}$ and downwards along -c are rotated in the opposite direction about $c$. Thus the orientation of the tetrahedra determined by the vertex parallel to $\mathbf{c}$ was considered to control the sign of the rotation. This coincidence does not appear in TMA-ZnI 4 .

The above-mentioned choice of tetrahedra rotations as an order parameter may help to explain the existence of modulated phases. An understanding


Fig. 5. Phase III, $\mathrm{ZnI}_{4}$ tetrahedra and $\mathrm{NC}_{4}$ tetrahedra, layer at $z=$ 0.25 .
of a modulation parallel to $\mathbf{b}$ or $\mathbf{c}$ requires additional mechanisms which favour one of the modulation directions for the different compounds before a final conclusion can be obtained.

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[^0]:    * Lists of structure factors, anisotropic atomic displacement parameters and H -atom parameters have been deposited with the British Library Document Supply Centre as Supplementary Publication No. SUP 52337 ( 42 pp.). Copies may be obtained through The Technical Editor, International Union of Crystallography, 5 Abbey Square, Chester CH1 2HU, England.

